

Sat-NeRF: Learning Multi-View Satellite Photogrammetry With Transient Objects and Shadow Modeling Using RPC Cameras

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Contributions

- ▶ A NeRF variant robust to the radiometric inconsistencies of multi-date satellite images, like shadows caused by the sun and small transient objects.
- ▶ Study the advantages of a clever use of satellite RPC camera models to increase the performance of NeRF architectures for satellite images.

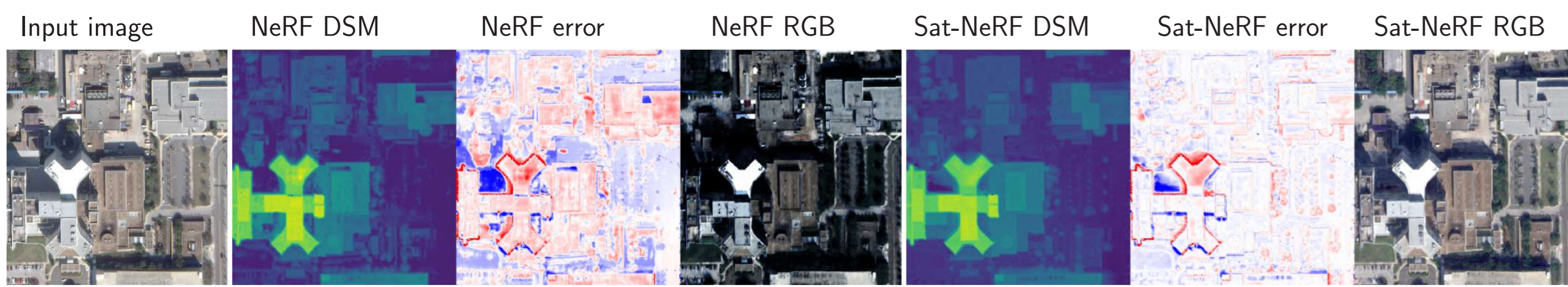


Figure 1: RGB renderings and surface models learned with NeRF and Sat-NeRF.

Architecture and fundamentals

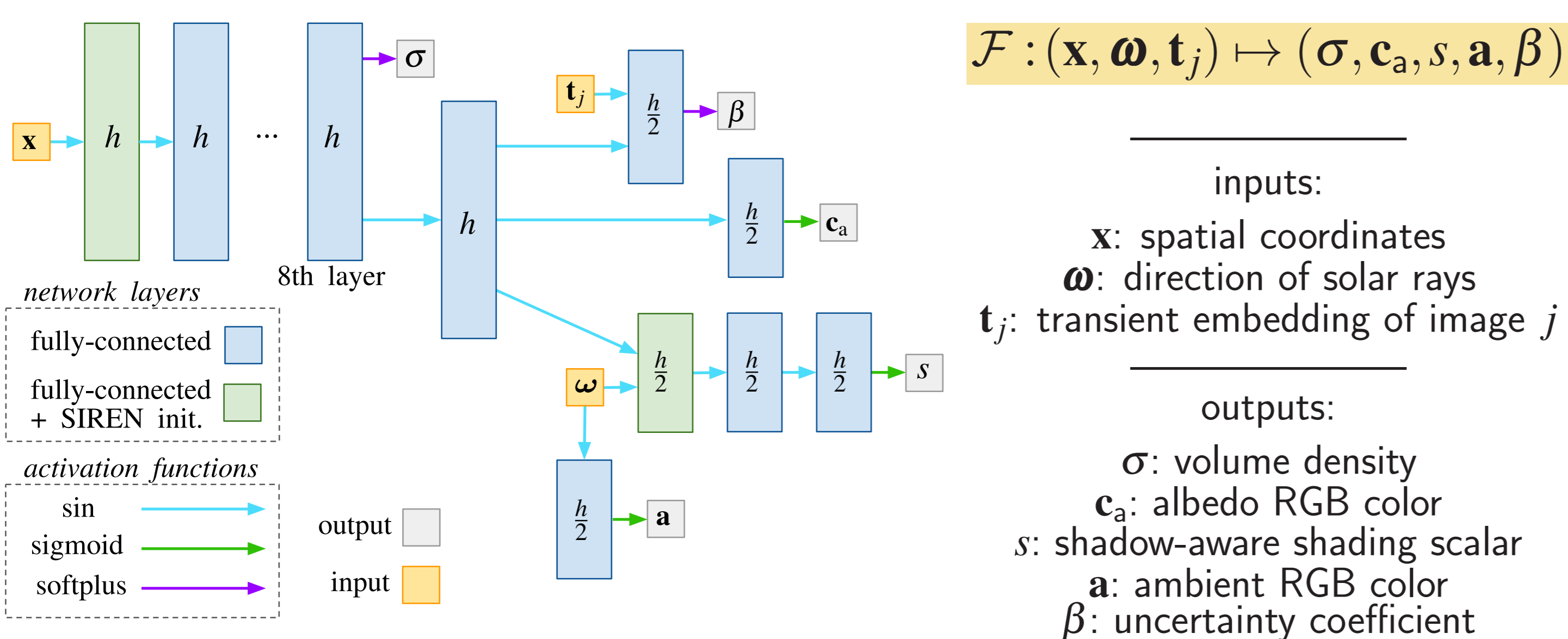


Figure 2: Sat-NeRF MLP architecture.

Sat-NeRF is trained using the volume rendering strategy of NeRF [1]. Each ray \mathbf{r} of a batch \mathcal{R} is discretized into a set of points $\mathbf{x}_i = \mathbf{o} + t_i \mathbf{d}$, where $t_i \in [t_{\text{near}}, t_{\text{far}}]$, and \mathbf{o} and \mathbf{d} are the origin and direction vectors. The rendered color $\mathbf{c}(\mathbf{r})$ and depth $d(\mathbf{r})$ of \mathbf{r} are

$$\mathbf{c}(\mathbf{r}) = \sum_{i=1}^N T_i \alpha_i \mathbf{c}_i \quad d(\mathbf{r}) = \sum_{i=1}^N T_i \alpha_i t_i. \quad (1)$$

where \mathbf{c}_i is the color predicted at \mathbf{x}_i . Opacity α_i and transmittance T_i are obtained from the volume density σ_i and σ_j : $j < i$ (to handle occlusions).

The Sat-NeRF loss uses a color term L_{RGB} and two auxiliary solar correction L_{SC} and depth supervision L_{DS} terms, weighted with $\lambda_{\text{SC}}, \lambda_{\text{DS}} \in \mathbb{R}$:

$$L_{\text{RGB}}(\mathcal{R}) + \lambda_{\text{SC}} L_{\text{SC}}(\mathcal{R}_{\text{SC}}) + \lambda_{\text{DS}} L_{\text{DS}}(\mathcal{R}_{\text{DS}}) \quad (2)$$

Uncertainty weighting for transient objects

Similarly to [2] we let the MLP learn an uncertainty coefficient β that weights the contribution of each point to the color term of the loss.

$$L_{\text{RGB}}(\mathcal{R}) = \sum_{\mathbf{r} \in \mathcal{R}} \frac{\|\mathbf{c}(\mathbf{r}) - \mathbf{c}_{\text{GT}}(\mathbf{r})\|_2^2}{2\beta'(\mathbf{r})^2} + \left(\frac{\log \beta'(\mathbf{r}) + \eta}{2} \right) \quad (3)$$

where $\beta'(\mathbf{r}) = \beta(\mathbf{r}) + 0.05$ and $\eta = 3$ to prevent negative values.

$$\beta(\mathbf{r}) = \sum_{i=1}^N T_i \alpha_i \beta_i \quad (4)$$

Shadow-aware irradiance model

Color is learned as in [3], using a linear combination of an albedo color \mathbf{c}_a with a shading scalar s and ambient hue \mathbf{a} related to the solar direction $\boldsymbol{\omega}$.

$$\mathbf{c}_i = \mathbf{c}_a(\mathbf{x}) \cdot (s(\mathbf{x}, \boldsymbol{\omega}) + (1 - s(\mathbf{x}, \boldsymbol{\omega})) \cdot \mathbf{a}(\boldsymbol{\omega})), \quad (5)$$

The solar correction term is used to prevent instabilities in s :

$$L_{\text{SC}}(\mathcal{R}_{\text{SC}}) = \sum_{\mathbf{r} \in \mathcal{R}_{\text{SC}}} \left(\sum_{i=1}^{N_{\text{SC}}} (T_i - s_i)^2 + 1 - \sum_{i=1}^{N_{\text{SC}}} T_i \alpha_i s_i \right), \quad (6)$$

where the rays in \mathcal{R}_{SC} follow the solar direction $\boldsymbol{\omega}$.

Point sampling using RPC camera models

Given the predefined altitude boundaries $[h_{\text{max}}, h_{\text{min}}]$, the ray \mathbf{r} intersecting the pixel \mathbf{p} in image j corresponds to the line between the boundary points:

$$\mathbf{x}_{\text{start}} = \mathcal{L}_j(\mathbf{p}, h_{\text{max}})_{\text{ECEF}} \quad \mathbf{x}_{\text{end}} = \mathcal{L}_j(\mathbf{p}, h_{\text{min}})_{\text{ECEF}}, \quad (7)$$

where \mathcal{L}_j is the localization function of image j . All point coordinates are expressed in the interval $[-1, 1]$ using an offset and scaling normalization.

RPC refinement and depth supervision

Bundle adjustment is used to refine the RPCs of all training images [4]. Without this preprocessing step, we observe a loss of accuracy in all metrics.

The sparse point cloud used in the BA can be reused for depth supervision:

$$L_{\text{DS}}(\mathcal{R}_{\text{DS}}) = \sum_{\mathbf{r} \in \mathcal{R}_{\text{DS}}} w(\mathbf{r}) (d(\mathbf{r}) - \|\mathbf{X}(\mathbf{r}) - \mathbf{o}(\mathbf{r})\|_2)^2, \quad (8)$$

where $\|\mathbf{X}(\mathbf{r}) - \mathbf{o}(\mathbf{r})\|_2$ is the target depth of the BA point $\mathbf{X}(\mathbf{r})$. \mathcal{R}_{DS} is the set of rays intersecting BA points. $w(\mathbf{r})$ is a reprojection error aware weight.

Results

- ▶ Trained/tested using the IEEE GRSS Data Fusion Contest 2019 benchmark.

Area index	PSNR \uparrow				SSIM \uparrow				Altitude MAE [m] \downarrow			
	004	068	214	260	004	068	214	260	004	068	214	260
NeRF	17.93	10.26	15.26	14.95	0.559	0.536	0.736	0.443	3.327	2.591	2.691	3.257
S-NeRF + SC	26.14	24.07	24.93	21.24	0.871	0.891	0.943	0.825	1.472	1.374	2.406	2.299
Sat-NeRF	26.16	24.80	25.54	21.88	0.876	0.903	0.951	0.840	1.416	1.275	2.125	2.428
Sat-NeRF + SC	26.67	25.07	25.50	21.78	0.884	0.908	0.950	0.842	1.288	1.249	2.009	1.864
Sat-NeRF + SC (no BA)	21.55	22.87	24.53	20.96	0.571	0.874	0.942	0.816	1.577	1.392	2.176	1.875
Sat-NeRF + DS	26.43	25.27	25.69	21.94	0.879	0.913	0.952	0.842	1.420	1.298	1.714	1.624
Sat-NeRF + DS + SC	26.62	25.00	25.66	21.66	0.881	0.909	0.952	0.839	1.366	1.277	1.676	1.638
S2P (10 pairs) [5]	—	—	—	—	—	—	—	—	1.370	1.174	1.811	1.640

Table 1: Numerical results using the test images (unseen at training time). The best altitude MAE values are given gold \bullet , silver \bullet and bronze \bullet medals.

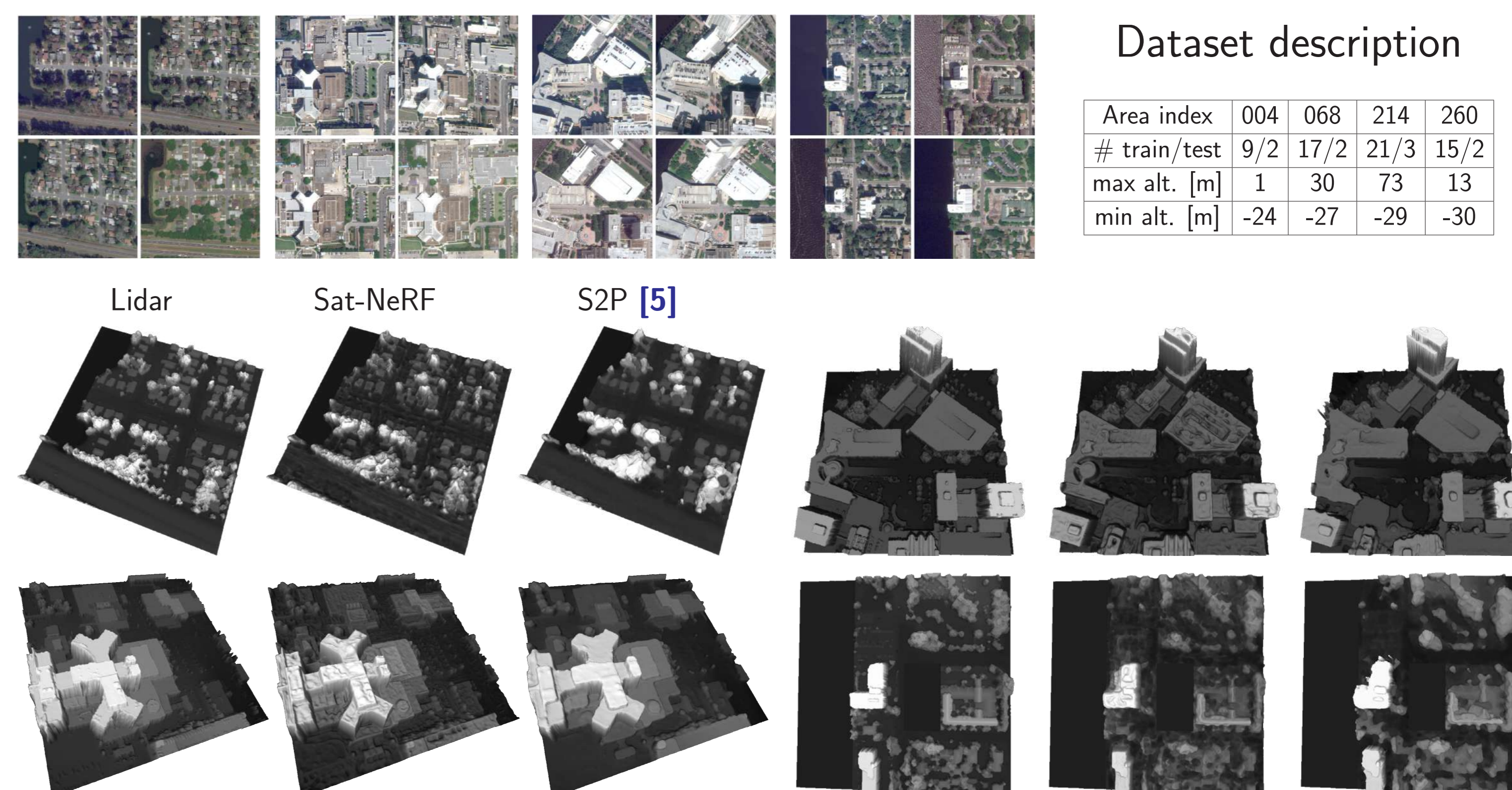


Figure 3: Compared to classic satellite MVS [5], Sat-NeRF surface models provide finer details and sharper structures but exhibit strong local irregularities.

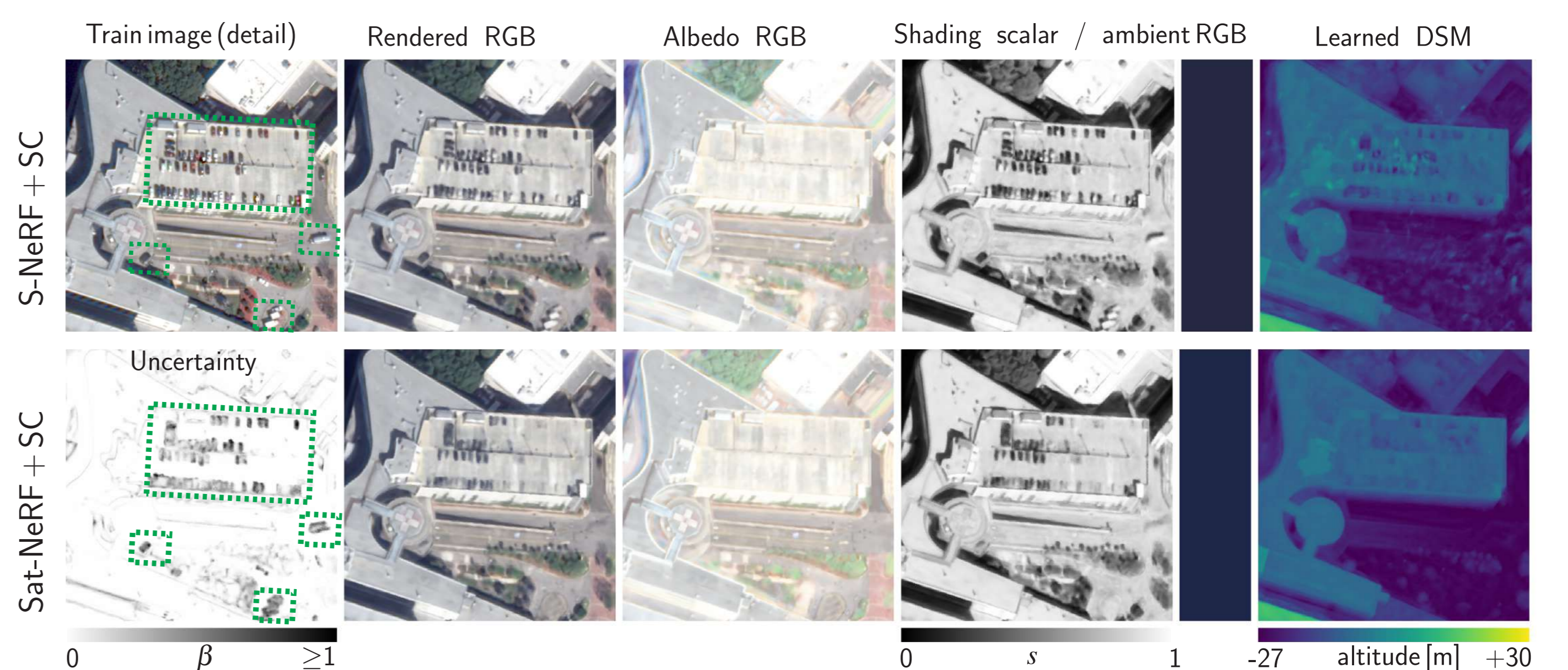


Figure 4: The uncertainty coefficient β learned by Sat-NeRF helps improve geometry learning with respect to previous NeRF variants for satellite images [3].

References

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- [2] Martin-Brualla, Ricardo et al. NeRF in the wild: Neural radiance fields for unconstrained photo collections. *CVPR*, 2021. doi.org/10.1109/CVPR46437.2021.00713
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- [4] Marí, Roger et al. A generic bundle adjustment methodology for indirect RPC model refinement of satellite imagery. *IPOLE*, 2021. doi.org/10.5201/ipo1.2021.352
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